



**June 2014**

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**Calculations for  
67, Brown Edge Rd  
Buxton**

**The following details have been determined following the carrying out of the attached calculations. These calculations were carried out using information following a site visit and from plans proposed.**

- **For purlin supports remove existing cavity wall and block or prop off either a 203 x 133 (25) UB or a 152 x 152 (30) UC sat on 450 x 150 x 100 reinforced padstones.**
- **For new purlins spanning 3.75m. use a 250 x 100 C24 timber for top purlin and a 225 x 75 C24 timber for bottom purlin.**
- **If existing purlins need to be extended use a system as shown in Figure 1 at end of calculations.**
- **For main decking frame use 150 x 50 C24 joists @ 450c/s on 225 x 75 C24 main cross supports on 150 x 150 posts on 0.5m x 0.5m concrete bases as shown in figure at end of calculations.**

**Any problems please ring the above office.**

**S. F Wherry**

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<b>Structural and Technical Systems Ltd 96, Green Lane Buxton Derbyshire SK17 9DJ Tel 01298 71761 Mobile 07973 711589</b>	<b>Job:-  Calculations for 67 Brown Edge Rd Buxton</b>	<b>Page:- 1</b>
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		<b>Calcs by:- SFW</b>

## **Loadings                      kN/m<sup>2</sup>**

### **Roof**

**Dead 1.1**

**Live 0.8                      1.9**

### **Decking floor**

**Live        1.5**

**Dead       0.5                      2.0**

## **Loadings**

The loadings are as shown in the attached drawings. It is presumed that the existing gable will be taken down and the purlins either propped with minimum 150 x 100 timbers or lightweight blockwork. The middle wall in the bungalow is loadbearing and the beams are designed as single span to sit on this.

The main structural layout of the decking is also shown on the attached drawings

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## Steel supports

Effective span 4.1m.

This beam basically carries two purlin loads and some slight blockwork load of average 0.75m. which will provide a factor of safety.

Bottom dead purlin point load  $3.5 \times 1.3 \times 1.1 = 5$

Bottom live purlin load  $3.5 \times 1.3 \times 0.8 = 3.65$

Top dead purlin point load  $3.5 \times 2.1 \times 1.1 = 8.1$

Bottom live purlin load  $3.5 \times 2.1 \times 0.8 = 5.9$

**From Pages C1 – C12 use either a 203 x 133 (25) UB  
or a 152 x 152 (23) UC sat on 450 x 150 x 100  
reinforced padstones.**

## Padstone design for under beams

Maximum factored shear force = 46kN

Actual stress with padstones below =  $\frac{4610^3}{450 \times 100}$

= 1.02 N/mm<sup>2</sup>

Allowable stress with brick =  $\frac{1.25 f_k}{\gamma_m} = \frac{1.25 \times 6.4}{3.1} = 2.58 \text{ N/mm}^2 \text{ O.K}$

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## **Existing purlin strengthening**

**Existing size approx. 175 x 50**

**Shear at one end = 9kN**

**Design connection as shown in Figure 1 at end of calculations**

## **Purlin for new roof area**

**Maximum span 3.75m**

**Dead load carried on upper purlin  $2.1 \times 1.1 = 2.3$  ( 1.40 on lower)**

**Live load  $2.1 \times 0.8 = 1.7$  ( 1.0 lower)**

**From Pages C13 – C18 use a 250 x 100 C24 timber sat upright for top purlin and 225 x 75 C24 timber for bottom purlin ( def'n do exceed codes by 2mm but should be considered adequate).**

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## Decking

Worst joist position is for possible cantilever at end

$$B.M. = 1.5 \times 1.5/2 \times 0.45 \times 2 = 1.01$$

With C24 timber

$$Z_{reqd} = 1.01 \times 10^6 / 7.5 = 1.35 \times 10^5$$

With 150 x 50

$$Z_{act} = 150 \times 150 \times 50 / 6 = 1.88 \times 10^5 \text{ O.K.}$$

**For joists use 150 x 50 C24 joists @ 450c/s**

Max. span of support beam 2.7m

$$\text{Load} = 4.6/2 \times 2 = 4.6 \text{ kN/m run (1.15 dead, 3.45 live)}$$

**From Pages C19 – C22 use 225 x 75 C24 timber for main supports**

$$\text{For posts maximum load} = 1.25 \times 12.42 = 15.5 \text{ kN}$$

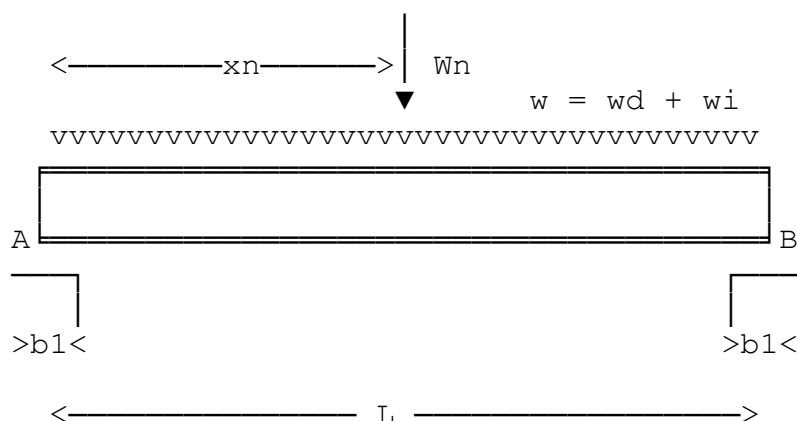
$$\text{Say max. height} = 1.8 \text{ m}$$

**From Pages C23 – C25 use 150 x 150 C24 timber for main posts on 0.5 x 0.5 concrete bases.**

Location: Brown Edge Rd

Simply supported steel beam subject to lateral torsional buckling

Calculations are in accordance with BS5950-1:2000. Simple beam with intermediate lateral restraints in accordance with Clause 4.3.5.2.



The n'th point load is shown:

$$W_n = W_{nd} + W_{ni}$$

where suffices:

d denotes dead

i denotes imposed

The moment capacity of the section is determined from 4.2.5.2 or 4.2.5.3 and is based on the classification obtained from Table 11.

Beam span  $L=4.1$  m

#### Section properties

203 x 133 x 25 UB.

Dimensions (mm):  $D=203.2$   $B=133.2$   $t=5.7$   $T=7.8$   $r=7.6$

Properties (cm):  $I_x=2340$   $I_y=308$   $S_x=258$   $S_y=70.9$   $J=5.96$

$A=32$   $r_y=3.1024$   $r_x=8.5513$

#### Strength of steel - Clause 3.1.1

The material thickness is 7.8mm and the steel grade is S 275.

Design strength  $p_y=275$  N/mm<sup>2</sup>

Young's Modulus  $E=205$  kN/mm<sup>2</sup>

#### Loading (unfactored)

Dead UDL (including S.W)  $w_d=1.7$  kN/m

Imposed UDL  $w_i=0$  kN/m

Dead point load 1 (+ve down)  $W_{1d}=5$  kN

Imposed point load 1  $W_{1i}=3.65$  kN

Distance from L.H. supp to load 1  $x_1=1.3$  m

Dead point load 2  $W_{2d}=8.1$  kN

Imposed point load 2  $W_{2i}=5.9$  kN

Distance from L.H. supp to load 2  $x_2=2.7$  m

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### Factored loads

Distributed load  $w' = w_d * 1.4 + w_i * 1.6 = 1.7 * 1.4 + 0 * 1.6$   
 $= 2.38 \text{ kN/m}$

Point load 1  $W1' = W1d * 1.4 + W1i * 1.6 = 5 * 1.4 + 3.65 * 1.6$   
 $= 12.84 \text{ kN}$

Point load 2  $W2' = W2d * 1.4 + W2i * 1.6 = 8.1 * 1.4 + 5.9 * 1.6$   
 $= 20.78 \text{ kN}$

### Factored shear force

At end B  $F_{vb} = w' * L / 2 + (W1' * x1 + W2' * x2) / L$   
 $= 2.38 * 4.1 / 2 + (12.84 * 1.3 + 20.78 * 2.7) / 4.1$   
 $= 22.635 \text{ kN}$

At end A  $F_{va} = w' * L + W1' + W2' - F_{vb}$   
 $= 2.38 * 4.1 + 12.84 + 20.78 - 22.635$   
 $= 20.743 \text{ kN}$

Max shear is at end B  $F_{ve} = F_{vb} = 22.635 \text{ kN}$

### Unfactored end shears

At end B dead  $F_{udb} = w_d * L / 2 + (W1d * x1 + W2d * x2) / L$   
 $= 1.7 * 4.1 / 2 + (5 * 1.3 + 8.1 * 2.7) / 4.1$   
 $= 10.405 \text{ kN}$

At end B imposed  $F_{uib} = w_i * L / 2 + (W1i * x1 + W2i * x2) / L$   
 $= 0 * 4.1 / 2 + (3.65 * 1.3 + 5.9 * 2.7) / 4.1$   
 $= 5.0427 \text{ kN}$

At end A dead  $F_{uda} = w_d * L + W1d + W2d - F_{udb}$   
 $= 1.7 * 4.1 + 5 + 8.1 - 10.405$   
 $= 9.6655 \text{ kN}$

At end A imposed  $F_{uia} = w_i * L + W1i + W2i - F_{uib}$   
 $= 0 * 4.1 + 3.65 + 5.9 - 5.0427$   
 $= 4.5073 \text{ kN}$

### Factored moment

Moment at load W1 (+ve sagging)  $M1 = F_{va} * x1 - w' * x1^2 / 2$   
 $= 20.743 * 1.3 - 2.38 * 1.3^2 / 2$   
 $= 24.955 \text{ kNm}$

Shear to left of W1  $F_l = F_{va} - w' * x1 = 20.743 - 2.38 * 1.3$   
 $= 17.649 \text{ kN}$

Shear to right of W1  $F_r = F_{va} - w' * x1 - W1'$   
 $= 20.743 - 2.38 * 1.3 - 12.84$   
 $= 4.8094 \text{ kN}$

Moment at load W2 (+ve sagging)  $M2 = F_{va} * x2 - W1' * (x2 - x1) - w' * x2^2 / 2$   
 $= 20.743 * 2.7 - 12.84 * (2.7 - 1.3) - 2.38 * 2.7^2 / 2$   
 $= 29.356 \text{ kNm}$

Shear to left of W2  $F_l = F_{va} - W1' - w' * x2$   
 $= 20.743 - 12.84 - 2.38 * 2.7$   
 $= 1.4774 \text{ kN}$

Shear to right of W2  $F_r = F_{va} - w' * x2 - W1' - W2'$   
 $= 20.743 - 2.38 * 2.7 - 12.84 - 20.78$   
 $= -19.303 \text{ kN}$

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Maximum BM occurs at 2nd load  $M=M_2=29.356$  kNm  
Corresponding shear force  $F=-F_r=19.303$  kN

#### Classification - Clause 3.5.2

Classify outstand element of compression flange:

Parameter (Table 11 Note b)  $e=(275/p_y)^{0.5}=(275/275)^{0.5}$   
 $=1$

Outstand  $b=B/2=133.2/2=66.6$  mm

Ratio  $b'T=b/T=66.6/7.8=8.5385$

As  $b/T \leq 9e$  ( 9 ), outstand element of compression flange is classified as Class 1 plastic.

Classify web of section:

Depth between fillet radii  $d=D-2*(T+r)=203.2-2*(7.8+7.6)$   
 $=172.4$  mm

Ratio  $d't=d/t=172.4/5.7=30.246$

Neutral axis is assumed to be at mid-depth of section.

As  $d/t \leq 80e$  ( 80 ), web is classified as Class 1 plastic.

#### Shear buckling

Since  $d/t < 70e$  no check for shear buckling is required.

#### Buckling resistance

Since the beam is subject to possible lateral torsional buckling, the buckling resistance moment  $M_b$  is first considered rather than the moment capacity  $M_c$  as a guide to selection.

#### Effective length - Clause 4.3.5.2

Beam is assumed to be laterally restraint at supports only.

Length of beam between restraints  $LT=L=4.1$  m

In accordance with Clause 4.3.5.2 for beams with effective lateral restraints at intervals within their length subject to normal loading conditions

Effective length  $Le=LT=4.1$  m

#### Clause 4.3.6.6 and Table 18

#### Equivalent uniform moment factor

The member is not loaded between restraints.

Maximum moment on segment  $M_e=29$  kNm

Far end BM  $\beta_e M=24$  kNm

Table 18 beta factor  $\beta_e=\beta_e M/M_e=24/29=0.82759$

Equivalent uniform moment factor  $m_{LT}=\text{TABLE 18 for } \beta_e=0.82759$   
 $=0.93103$



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Resistance to lateral-torsional buckling - Clause 4.3.6

Radius gyration about minor axis  $r_y = \sqrt{I_y/A} = \sqrt{308/32}$   
= 3.1024 cm

Slenderness of section  $\lambda = l_e/r_y * 100 = 4.1/3.1024 * 100$   
= 132.15

Buckling parameter  $u = (4 * S_x^2 * (1 - I_y/I_x) / (A^2 * ((D-T)/10)^2))^0.25$   
=  $(4 * 258^2 * (1 - 308/2340) / (32^2 * ((203.2 - 7.8)/10)^2))^0.25$   
= 0.87693

Torsional index  $x = 0.566 * ((D-T)/10) * (A/J)^0.5$   
=  $0.566 * ((203.2 - 7.8)/10) * (32/5.96)^0.5$   
= 25.627

Ratio  $ratio = \lambda/x = 132.15/25.627$   
= 5.1569

Slenderness factor  $v = 1 / ((1 + 0.05 * ratio^2)^0.25)$   
=  $1 / ((1 + 0.05 * 5.1569^2)^0.25)$   
= 0.80942

Ratio  $\beta_w$   $betaw = 1.0$

Equivalent slenderness  $\lambda_{mLT} = u * v * \lambda * (betaw)^0.5$   
=  $0.87693 * 0.80942 * 132.15 * (1)^0.5$   
= 93.804

Limiting slenderness  $\lambda_{mlo} = 0.4 * ((\pi^2 * E * 10^3) / p_y)^0.5$   
=  $0.4 * ((3.1416^2 * 205 * 10^3) / 275)^0.5$   
= 34.31

Perry coefficient  $\eta_{LT} = 0.007 * (\lambda_{mLT} - \lambda_{mlo})$   
=  $0.007 * (93.804 - 34.31)$   
= 0.41646

Elastic strength  $p_e = \pi^2 * E * 10^3 / (\lambda_{mLT}^2)$   
=  $3.1416^2 * 205 * 10^3 / (93.804^2)$   
= 229.94 N/mm<sup>2</sup>

Factor  $\phi_{LT} = (p_y + (\eta_{LT} + 1) * p_e) / 2$   
=  $(275 + (0.41646 + 1) * 229.94) / 2$   
= 300.35 N/mm<sup>2</sup>

Factor  $p_{ey} = p_e * p_y = 229.94 * 275 = 63232$

Bending strength  $p_b = (p_{ey}) / (\phi_{LT} + ((\phi_{LT}^2 - p_{ey})^0.5))$   
=  $(63232) / (300.35 + ((300.35^2 - 63232)^0.5))$   
= 136.1 N/mm<sup>2</sup>

Buckling resistance moment  $M_b = S_x * p_b / 10^3 = 258 * 136.1 / 10^3$   
= 35.115 kNm

Equivalent uniform moment factor  $m_{LT} = 0.93103$

Since  $M \leq M_b / m_{LT}$  ( 29.356 kNm  $\leq$  37.716 kNm ), section OK for lateral torsional buckling resistance.

Check section for combined moment and shear

Maximum moment and co-existent shear

Shear area  $A_v = t * D = 5.7 * 203.2 = 1158.2 \text{ mm}^2$

Shear capacity  $P_v = 0.6 * p_y * A_v / 10^3 = 0.6 * 275 * 1158.2 / 10^3$   
= 191.11 kN

Design shear force  $F_v = F = 19.303 \text{ kN}$

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Elastic modulus  $Z = I_x / (D/20) = 2340 / (203.2/20)$   
 $= 230.31 \text{ cm}^3$

Since  $F_v < 0.6 P_v$

Moment capacity for compact sec  $M_c = p_y \cdot S_x / 10^3 = 275 \cdot 258 / 10^3$   
 $= 70.95 \text{ kNm}$

Since  $M \leq M_c$  (  $29.356 \text{ kNm} \leq 70.95 \text{ kNm}$  ), applied moment within moment capacity.

#### Maximum shear and coexistent moment

Shear capacity  $P_v = 191.11 \text{ kN}$

Design shear force  $F_v = F_{ve} = 22.635 \text{ kN}$

Coexistent moment  $M' = 0 \text{ kNm}$

Since  $F_v \leq P_v$  (  $22.635 \text{ kN} \leq 191.11 \text{ kN}$  ), shear force within shear capacity.

#### Check for deflection

Imposed load only considered in deflection calculation

UDL for deflection calculation  $w_u = w_i = 0 \text{ kN/m}$

Central UDL defln  $DEL_w = 5 \cdot w_u \cdot L^4 / (384 \cdot E \cdot I_x) \cdot 10^5$   
 $= 5 \cdot 0 \cdot 4.1^4 / (384 \cdot 205 \cdot 2340) \cdot 10^5$   
 $= 0 \text{ mm}$

Constant for defln  $const = L^3 \cdot 10^5 / (48 \cdot E \cdot I_x)$   
 $= 4.1^3 \cdot 10^5 / (48 \cdot 205 \cdot 2340)$   
 $= 0.29932$

Distance for defln  $a = x_1 = 1.3 \text{ m}$

Point load 1 for defln calc  $W_1 = W_{1i} = 3.65 \text{ kN}$

Centl defln for  $W_1$   $DEL_{W1} = (3 \cdot a / L - 4 \cdot (a / L)^3) \cdot W_1 \cdot const$   
 $= (3 \cdot 1.3 / 4.1 - 4 \cdot (1.3 / 4.1)^3) \cdot 3.65$   
 $\cdot 0.29932$   
 $= 0.89993 \text{ mm}$

Distance for defln  $a = L - x_2 = 4.1 - 2.7 = 1.4 \text{ m}$

Point load 2 for defln calc  $W_2 = W_{2i} = 5.9 \text{ kN}$

Centl defln for  $W_2$   $DEL_{W2} = (3 \cdot a / L - 4 \cdot (a / L)^3) \cdot W_2 \cdot const$   
 $= (3 \cdot 1.4 / 4.1 - 4 \cdot (1.4 / 4.1)^3) \cdot 5.9$   
 $\cdot 0.29932$   
 $= 1.5278 \text{ mm}$

Total central defln  $DEL = DEL_w + DEL_{W1} + DEL_{W2} = 0 + 0.89993 + 1.5278$   
 $= 2.4278 \text{ mm}$

From Table 8

Limiting deflection ( brittle )  $DEL_{lim} = L \cdot 1000 / 360 = 4.1 \cdot 1000 / 360$   
 $= 11.389 \text{ mm}$

Since  $DEL \leq DEL_{lim}$  (  $2.4278 \text{ mm} \leq 11.389 \text{ mm}$  ) OK for deflection.

SECTION	203 x 133 x 25 UKB Grade S 275
	Shear force 22.635 kN
DESIGN	Shear capacity 191.11 kN
SUMMARY	Max. applied moment 29.356 kNm
	Moment capacity 70.95 kNm
	Buckling resistance 35.115 kNm
	Moment factor (mLT) 0.93103
	Resistance (Mb/mLT) 37.716 kNm
	Deflection 2.4278 mm
	Limiting deflection 11.389 mm
	DL shear at A 9.6655 kN
	LL shear at A 4.5073 kN

Unfactored

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Structural alterations

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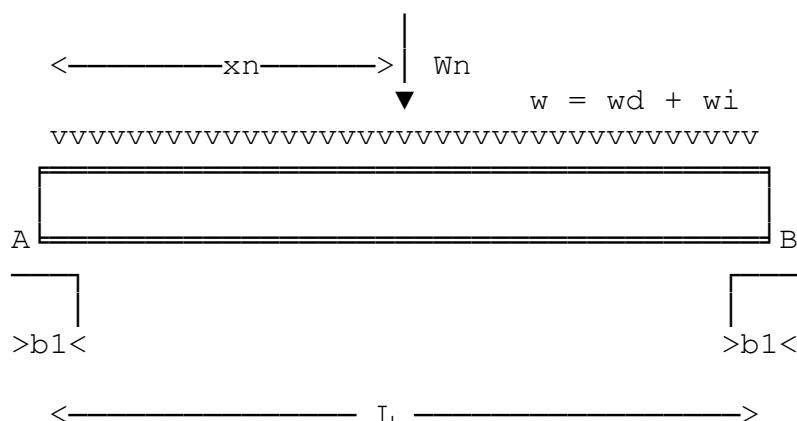
end shears | DL shear at B  
                  | LL shear at B

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10.405 kN  
5.0427 kN

Location: Brown Edge Rd

Simply supported steel beam subject to lateral torsional buckling

Calculations are in accordance with BS5950-1:2000. Simple beam with intermediate lateral restraints in accordance with Clause 4.3.5.2.



The n'th point load  
is shown:

$$W_n = W_{nd} + W_{ni}$$

where suffices:

d denotes dead

i denotes imposed

The moment capacity of the section is determined from 4.2.5.2 or 4.2.5.3 and is based on the classification obtained from Table 11.

Beam span L=4.1 m

## Section properties

152 x 152 x 30 UC.

Dimensions (mm): D=157.6 B=152.9 t=6.5 T=9.4 r=7.6

Properties (cm): Ix=1750 Iy=560 Sx=248 Sy=112 J=10.5

A=38.3 ry=3.8238 rx=6.7596

## Strength of steel - Clause 3.1.1

The material thickness is 9.4 mm and the steel grade is S 275.

Design strength  $p_y = 275 \text{ N/mm}^2$

Young's Modulus  $E=205 \text{ kN/mm}^2$

## Loading (unfactored)

Dead UDL (including S.W) wd=1.7 kN/m

Imposed UDL  $w_i=0$  kN/m

Dead point load 1 (+ve down) W1d=5 kN

Imposed point load 1 W1i=3.65 kN

Distance from L.H. supp to load 1  $x_1=1.3$  m

Dead point load 2 W2d=8.1 kN

Imposed point load 2  $W_{2i}=5.9 \text{ kN}$

Distance from L.H. supp to load 2  $x_2=2.7$  m

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### Factored loads

Distributed load

$$w' = w_d * 1.4 + w_i * 1.6 = 1.7 * 1.4 + 0 * 1.6 \\ = 2.38 \text{ kN/m}$$

Point load 1

$$W1' = W1d * 1.4 + W1i * 1.6 = 5 * 1.4 + 3.65 * 1.6 \\ = 12.84 \text{ kN}$$

Point load 2

$$W2' = W2d * 1.4 + W2i * 1.6 = 8.1 * 1.4 + 5.9 * 1.6 \\ = 20.78 \text{ kN}$$

### Factored shear force

At end B

$$F_{vb} = w' * L / 2 + (W1' * x1 + W2' * x2) / L \\ = 2.38 * 4.1 / 2 + (12.84 * 1.3 + 20.78 * 2.7) / 4.1 \\ = 22.635 \text{ kN}$$

At end A

$$F_{va} = w' * L + W1' + W2' - F_{vb} \\ = 2.38 * 4.1 + 12.84 + 20.78 - 22.635 \\ = 20.743 \text{ kN}$$

Max shear is at end B

$$F_{ve} = F_{vb} = 22.635 \text{ kN}$$

### Unfactored end shears

At end B dead

$$F_{udb} = w_d * L / 2 + (W1d * x1 + W2d * x2) / L \\ = 1.7 * 4.1 / 2 + (5 * 1.3 + 8.1 * 2.7) / 4.1 \\ = 10.405 \text{ kN}$$

At end B imposed

$$F_{uib} = w_i * L / 2 + (W1i * x1 + W2i * x2) / L \\ = 0 * 4.1 / 2 + (3.65 * 1.3 + 5.9 * 2.7) / 4.1 \\ = 5.0427 \text{ kN}$$

At end A dead

$$F_{uda} = w_d * L + W1d + W2d - F_{udb} \\ = 1.7 * 4.1 + 5 + 8.1 - 10.405 \\ = 9.6655 \text{ kN}$$

At end A imposed

$$F_{uia} = w_i * L + W1i + W2i - F_{uib} \\ = 0 * 4.1 + 3.65 + 5.9 - 5.0427 \\ = 4.5073 \text{ kN}$$

### Factored moment

Moment at load W1 (+ve sagging)

$$M1 = F_{va} * x1 - w' * x1^2 / 2 \\ = 20.743 * 1.3 - 2.38 * 1.3^2 / 2 \\ = 24.955 \text{ kNm}$$

Shear to left of W1

$$F_l = F_{va} - w' * x1 = 20.743 - 2.38 * 1.3 \\ = 17.649 \text{ kN}$$

Shear to right of W1

$$F_r = F_{va} - w' * x1 - W1' \\ = 20.743 - 2.38 * 1.3 - 12.84 \\ = 4.8094 \text{ kN}$$

Moment at load W2 (+ve sagging)

$$M2 = F_{va} * x2 - W1' * (x2 - x1) - w' * x2^2 / 2 \\ = 20.743 * 2.7 - 12.84 * (2.7 - 1.3) - 2.38 \\ * 2.7^2 / 2 \\ = 29.356 \text{ kNm}$$

Shear to left of W2

$$F_l = F_{va} - W1' - w' * x2 \\ = 20.743 - 12.84 - 2.38 * 2.7 \\ = 1.4774 \text{ kN}$$

Shear to right of W2

$$F_r = F_{va} - w' * x2 - W1' - W2' \\ = 20.743 - 2.38 * 2.7 - 12.84 - 20.78 \\ = -19.303 \text{ kN}$$

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Maximum BM occurs at 2nd load  $M=M_2=29.356$  kNm  
Corresponding shear force  $F=-F_r=19.303$  kN

#### Classification - Clause 3.5.2

Classify outstand element of compression flange:

Parameter (Table 11 Note b)  $e=(275/p_y)^{0.5}=(275/275)^{0.5}$   
 $=1$

Outstand  $b=B/2=152.9/2=76.45$  mm

Ratio  $b'T=b/T=76.45/9.4=8.133$

As  $b/T \leq 9e$  ( 9 ), outstand element of compression flange is classified as Class 1 plastic.

Classify web of section:

Depth between fillet radii  $d=D-2*(T+r)=157.6-2*(9.4+7.6)$   
 $=123.6$  mm

Ratio  $d't=d/t=123.6/6.5=19.015$

Neutral axis is assumed to be at mid-depth of section.

As  $d/t \leq 80e$  ( 80 ), web is classified as Class 1 plastic.

#### Shear buckling

Since  $d/t < 70e$  no check for shear buckling is required.

#### Buckling resistance

Since the beam is subject to possible lateral torsional buckling, the buckling resistance moment  $M_b$  is first considered rather than the moment capacity  $M_c$  as a guide to selection.

#### Effective length - Clause 4.3.5.2

Beam is assumed to be laterally restraint at supports only.

Length of beam between restraints  $LT=L=4.1$  m

In accordance with Clause 4.3.5.2 for beams with effective lateral restraints at intervals within their length subject to normal loading conditions

Effective length  $Le=LT=4.1$  m

#### Clause 4.3.6.6 and Table 18

#### Equivalent uniform moment factor

The member is not loaded between restraints.

Maximum moment on segment  $Me=29$  kNm

Far end BM  $\beta M=24$  kNm

Table 18 beta factor  $\beta=\beta M/Me=24/29=0.82759$

Equivalent uniform moment factor  $m_{LT}=\text{TABLE 18 for } \beta=0.82759$   
 $=0.93103$

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Resistance to lateral-torsional buckling - Clause 4.3.6

Radius gyration about minor axis  $r_y = \sqrt{I_y/A} = \sqrt{560/38.3}$   
= 3.8238 cm

Slenderness of section  $\lambda = L_e/r_y \cdot 100 = 4.1/3.8238 \cdot 100$   
= 107.22

Buckling parameter  $u = (4 \cdot S_x^2 \cdot (1 - I_y/I_x) / (A^2 \cdot ((D-T)/10)^2))^{\wedge 0.25}$   
=  $(4 \cdot 248^2 \cdot (1 - 560/1750) / (38.3^2 \cdot ((157.6 - 9.4)/10)^2))^{\wedge 0.25}$   
= 0.84888

Torsional index  $x = 0.566 \cdot ((D-T)/10) \cdot (A/J)^{\wedge 0.5}$   
=  $0.566 \cdot ((157.6 - 9.4)/10) \cdot (38.3/10.5)^{\wedge 0.5}$   
= 16.02

Ratio  $\text{ratio} = \lambda/x = 107.22/16.02$   
= 6.693

Slenderness factor  $v = 1 / ((1 + 0.05 \cdot \text{ratio}^2)^{\wedge 0.25})$   
=  $1 / ((1 + 0.05 \cdot 6.693^2)^{\wedge 0.25})$   
= 0.74537

Ratio  $\beta_w$   $\text{betaw} = 1.0$

Equivalent slenderness  $\lambda_{LT} = u \cdot v \cdot \lambda \cdot (\text{betaw})^{\wedge 0.5}$   
=  $0.84888 \cdot 0.74537 \cdot 107.22 \cdot (1)^{\wedge 0.5}$   
= 67.843

Limiting slenderness  $\lambda_{lo} = 0.4 \cdot ((\pi^2 \cdot E \cdot 10^3) / p_y)^{\wedge 0.5}$   
=  $0.4 \cdot ((3.1416^2 \cdot 205 \cdot 10^3) / 275)^{\wedge 0.5}$   
= 34.31

Perry coefficient  $\eta_{LT} = 0.007 \cdot (\lambda_{LT} - \lambda_{lo})$   
=  $0.007 \cdot (67.843 - 34.31)$   
= 0.23473

Elastic strength  $p_e = \pi^2 \cdot E \cdot 10^3 / (\lambda_{LT}^2)$   
=  $3.1416^2 \cdot 205 \cdot 10^3 / (67.843^2)$   
= 439.59 N/mm<sup>2</sup>

Factor  $\phi_{LT} = (p_y + (\eta_{LT} + 1) \cdot p_e) / 2$   
=  $(275 + (0.23473 + 1) \cdot 439.59) / 2$   
= 408.89 N/mm<sup>2</sup>

Factor  $p_{ey} = p_e \cdot p_y = 439.59 \cdot 275 = 120887$

Bending strength  $p_b = (p_{ey}) / (\phi_{LT} + ((\phi_{LT}^2 - p_{ey})^{\wedge 0.5}))$   
=  $(120887) / (408.89 + ((408.89^2 - 120887)^{\wedge 0.5}))$   
= 193.71 N/mm<sup>2</sup>

Buckling resistance moment  $M_b = S_x \cdot p_b / 10^3 = 248 \cdot 193.71 / 10^3$   
= 48.04 kNm

Equivalent uniform moment factor  $m_{LT} = 0.93103$

Since  $M \leq M_b / m_{LT}$  ( 29.356 kNm  $\leq$  51.598 kNm ), section OK for lateral torsional buckling resistance.

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Check section for combined moment and shear

Maximum moment and co-existent shear

Shear area  $A_v = t \cdot D = 6.5 \cdot 157.6 = 1024.4 \text{ mm}^2$   
Shear capacity  $P_v = 0.6 \cdot p_y \cdot A_v / 10^3 = 0.6 \cdot 275 \cdot 1024.4 / 10^3 = 169.03 \text{ kN}$   
Design shear force  $F_v = F = 19.303 \text{ kN}$   
Elastic modulus  $Z = I_x / (D/20) = 1750 / (157.6/20) = 222.08 \text{ cm}^3$

Since  $F_v < 0.6 P_v$

Moment capacity for compact sec  $M_c = p_y \cdot S_x / 10^3 = 275 \cdot 248 / 10^3 = 68.2 \text{ kNm}$

Since  $M \leq M_c$  (  $29.356 \text{ kNm} \leq 68.2 \text{ kNm}$  ), applied moment within moment capacity.

Maximum shear and coexistent moment

Shear capacity  $P_v = 169.03 \text{ kN}$   
Design shear force  $F_v = F_{ve} = 22.635 \text{ kN}$   
Coexistent moment  $M' = 0 \text{ kNm}$   
Since  $F_v \leq P_v$  (  $22.635 \text{ kN} \leq 169.03 \text{ kN}$  ), shear force within shear capacity.

Check for deflection

Imposed load only considered in deflection calculation

UDL for deflection calculation  $w_u = w_i = 0 \text{ kN/m}$   
Central UDL defln  $DEL_w = 5 \cdot w_u \cdot L^4 / (384 \cdot E \cdot I_x) \cdot 10^5 = 5 \cdot 0 \cdot 4.1^4 / (384 \cdot 205 \cdot 1750) \cdot 10^5 = 0 \text{ mm}$

Constant for defln  $const = L^3 \cdot 10^5 / (48 \cdot E \cdot I_x) = 4.1^3 \cdot 10^5 / (48 \cdot 205 \cdot 1750) = 0.40024$

Distance for defln  $a = x_1 = 1.3 \text{ m}$   
Point load 1 for defln calc  $W_1 = W_{1i} = 3.65 \text{ kN}$   
Centl defln for  $W_1$   $DEL_{W1} = (3 \cdot a / L - 4 \cdot (a/L)^3) \cdot W_1 \cdot const = (3 \cdot 1.3 / 4.1 - 4 \cdot (1.3/4.1)^3) \cdot 3.65 \cdot 0.40024 = 1.2033 \text{ mm}$

Distance for defln  $a = L - x_2 = 4.1 - 2.7 = 1.4 \text{ m}$   
Point load 2 for defln calc  $W_2 = W_{2i} = 5.9 \text{ kN}$   
Centl defln for  $W_2$   $DEL_{W2} = (3 \cdot a / L - 4 \cdot (a/L)^3) \cdot W_2 \cdot const = (3 \cdot 1.4 / 4.1 - 4 \cdot (1.4/4.1)^3) \cdot 5.9 \cdot 0.40024 = 2.0429 \text{ mm}$

Total central defln  $DEL = DEL_w + DEL_{W1} + DEL_{W2} = 0 + 1.2033 + 2.0429 = 3.2463 \text{ mm}$

From Table 8

Limiting deflection ( brittle )  $DEL_{lim} = L \cdot 1000 / 360 = 4.1 \cdot 1000 / 360 = 11.389 \text{ mm}$

Since  $DEL \leq DEL_{lim}$  (  $3.2463 \text{ mm} \leq 11.389 \text{ mm}$  ) OK for deflection.

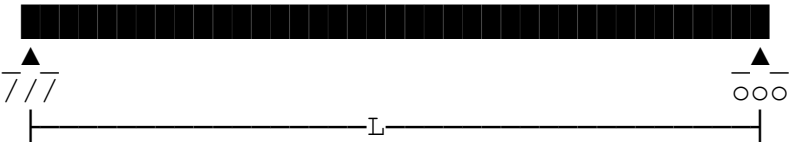


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SECTION	152 x 152 x 30 UKC Grade S 275
	Shear force 22.635 kN
DESIGN	Shear capacity 169.03 kN
SUMMARY	Max. applied moment 29.356 kNm
	Moment capacity 68.2 kNm
	Buckling resistance 48.04 kNm
	Moment factor (mLT) 0.93103
	Resistance (Mb/mLT) 51.598 kNm
	Deflection 3.2463 mm
	Limiting deflection 11.389 mm
Unfactored end shears	DL shear at A 9.6655 kN
	LL shear at A 4.5073 kN
	DL shear at B 10.405 kN
	LL shear at B 5.0427 kN

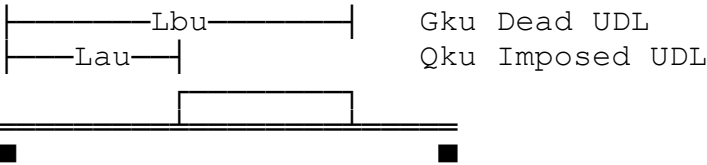
Location: Brown Edge

Timber beam to BS5268-2:2002



Simply supported  
beam subjected to  
vertical loads.

Beam span  $L=3.8\text{ m}$   
All loads are positive downwards, reactions are positive upwards,  
sagging moments are positive.



Distances are measured  
from left hand support

Uniformly distributed load 1 of 1  
Dist. from left support to start  $Lau(1)=0\text{ m}$   
Distance from left support to end  $Lbu(1)=3.8\text{ m}$   
Dead load (unfactored)  $Gku(1)=2.3\text{ kN/m}$   
Imposed load (unfactored)  $Qku(1)=1.7\text{ kN/m}$

BMs at 20th points, from left to right (sagging is positive)

0	1.3718	2.5992	3.6822	4.6208	5.415
	6.0648	6.5702	6.9312	7.1478	7.22
	7.1478	6.9312	6.5702	6.0648	5.415
	4.6208	3.6822	2.5992	1.3718	0

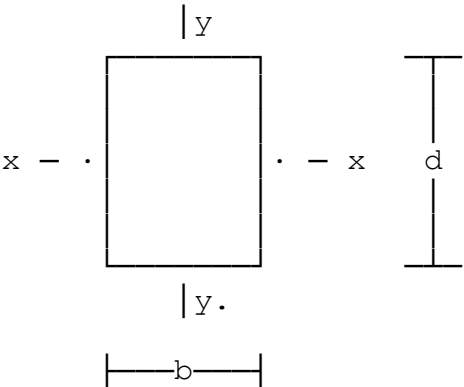
Maximum span bending moment  $7.22\text{ kNm}$

End shears

Shear force at left hand end  $7.6\text{ kN}$   
Shear force at right hand end  $7.6\text{ kN}$   
Design shear force  $F_{ve}'=7.6$

Unfactored dead shear at LHE  $4.37\text{ kN}$   
Unfactored imposed shear at LHE  $3.23\text{ kN}$   
Unfactored dead shear at RHE  $4.37\text{ kN}$   
Unfactored imposed shear at RHE  $3.23\text{ kN}$

Section design parameters



Design bending moment	M=7.22 kNm
Design shear force	Fve=7.6 kN
Design axial load (+ve compress)	Fa=0 kN
Depth of section	d=250 mm
Width of section	b=100 mm
Eff length for bending about xx	Lex=3800 mm
Eff length for bending about yy	Ley=0 mm
Length of bearing	lb=75 mm
From BS5268-2 Table 18, bearing is	< 75 mm from joist end.
Bearing Modification factor	K4=1.0
Strength class C24 to Table 8	
Timber service class adopted	tmclass=1
Timber service class modification factor	K2=1 as Table 16.
Modification factors:	
Bending parallel to grain	K2ben=1.0
Tension parallel to grain	K2ten=1.0
Compression parallel to grain	K2com=1.0
Compression $\perp$ to grain	K2per=1.0
Shear parallel to grain	K2shr=1.0
Mean & min modulus of elasticity	K2mod=1.0

#### Section properties

Inertia about xx axis	$I_x = b \cdot d^3 / 12 = 100 \cdot 250^3 / 12$ =130.21E6 mm <sup>4</sup>
Inertia about yy axis	$I_y = d \cdot b^3 / 12 = 250 \cdot 100^3 / 12$ =20.833E6 mm <sup>4</sup>
Area of cross section	A=b*d=100*250=25000 mm <sup>2</sup>
Radius of gyration about xx axis	$i_x = \sqrt{I_x / A} = \sqrt{130.21E6 / 25000}$ =72.169 mm
Radius of gyration about yy axis	$i_y = \sqrt{I_y / A} = \sqrt{20.833E6 / 25000}$ =28.868 mm

#### Slenderness

Slenderness ratio about xx axis	$\lambda_{bdx} = L_{ex} / i_x = 3800 / 72.169$ =52.654
Slenderness ratio about yy axis	$\lambda_{bdy} = L_{ey} / i_y = 0 / 28.868$ =0
xx axis controls slenderness at	$\lambda = \lambda_{bdx} = 52.654$

#### Grade stresses

Compression parallel to grain	cparg=7.9 N/mm <sup>2</sup>
Bending parallel to grain	bparg=7.5 N/mm <sup>2</sup>
Shear parallel to grain	sparg=0.71 N/mm <sup>2</sup>
Compression perp to grain	cperd=2.4 N/mm <sup>2</sup>
Mean modulus of elasticity	E <sub>mean</sub> =10800 N/mm <sup>2</sup>
Minimum modulus of elasticity	E <sub>min</sub> =7200 N/mm <sup>2</sup>

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### Modification factors

Duration of loading  $K3=1.25$   
Depth factor  $K7=(300/d)^{0.11}=(300/250)^{0.11}=1.0203$   
Member is not in a load-sharing system as defined by Clause 2.9.  
Modulus of elasticity  $E=E_{min}*K2_{mod}=7200*1=7200 \text{ N/mm}^2$   
Load-sharing modification factor  $K8=1.0$   
No notches exist at the support  $K5=1.0$

### Permissible stresses

Permissible bending stress  $\sigma_{mad}=K2_{ben}*K3*K7*K8*\sigma_{parg}$   
 $=1*1.25*1.0203*1*7.5$   
 $=9.5649 \text{ N/mm}^2$   
Shear parallel to grain  $\tau_{orad}=K2_{shr}*K3*K5*K8*\sigma_{parg}$   
 $=1*1.25*1*1*0.71$   
 $=0.8875 \text{ N/mm}^2$   
Compress perp to grain (no wane)  $\sigma_{bad}=K2_{per}*K3*K4*K8*\sigma_{cperd}$   
 $=1*1.25*1*1*2.4$   
 $=3 \text{ N/mm}^2$

### Bending

Applied bending stress  $\sigma=M*1E6*(d/2)/I_x$   
 $=7.22*1E6*(250/2)/130.21E6$   
 $=6.9312 \text{ N/mm}^2$

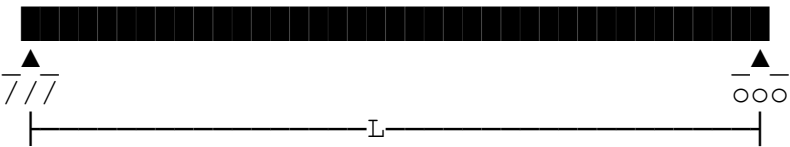
Since  $\sigma \leq \sigma_{mad}$  (  $6.9312 \text{ N/mm}^2 \leq 9.5649 \text{ N/mm}^2$  ) applied bending stress within permissible.

### Check for deflection (including shear defln as reqd by Clause 2.10.7)

Deflection based on  $E=7200 \text{ N/mm}^2$   
DL deflection without shear  $d_{ld}=d_{ld}=6.6609 \text{ mm}$   
Imposed deflection without shear  $i_{ld}=i_{ld}=4.9232 \text{ mm}$   
Total DL & imposed deflection  $11.584 \text{ mm}$   
Modulus of rigidity  $G=E/16=7200/16=450 \text{ N/mm}^2$   
Shape factor for rect section  $KF=1.2$   
Shear area for beam  $A_y=d*b/KF=250*100/1.2=20833 \text{ mm}^2$   
Total DL & imposed  $15.2 \text{ kN}$   
If total DL & imposed load applied as a UDL, additional deflection due to shear  $d_{su}=W T' * L * 10^6 / (8 * A_y * G)$   
 $=15.2 * 3.8 * 10^6 / (8 * 20833 * 450)$   
 $=0.77013 \text{ mm}$   
Shear deflection  $d_{els}=d_{su} * M / (W T' * L / 8)$   
 $=0.77013 * 7.22 / (15.2 * 3.8 / 8)$   
 $=0.77013 \text{ mm}$   
Limiting deflection  $DEL_{lim}=0.003 * L * 10^3 = 0.003 * 3.8 * 10^3$   
 $=11.4 \text{ mm}$   
Deflection inclusive of shear  $DEL=d_{ld}+i_{ld}+d_{els}$   
 $=6.6609+4.9232+0.77013$   
 $=12.354 \text{ mm}$   
Since  $DEL > DEL_{lim}$  (  $12.354 \text{ mm} > 11.4 \text{ mm}$  ), deflection exceeds limiting value.

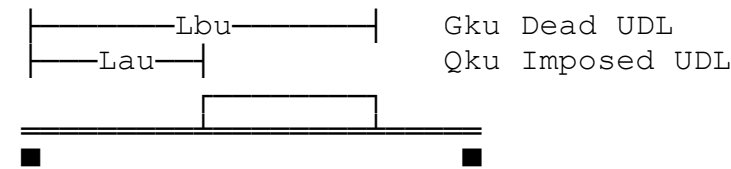
Location: Brown Edge

Timber beam to BS5268-2:2002



Simply supported  
beam subjected to  
vertical loads.

Beam span  $L=3.8\text{ m}$   
All loads are positive downwards, reactions are positive upwards,  
sagging moments are positive.



Distances are measured  
from left hand support

Uniformly distributed load 1 of 1  
Dist. from left support to start  $Lau(1)=0\text{ m}$   
Distance from left support to end  $Lbu(1)=3.8\text{ m}$   
Dead load (unfactored)  $Gku(1)=1.4\text{ kN/m}$   
Imposed load (unfactored)  $Qku(1)=1.0\text{ kN/m}$

BMs at 20th points, from left to right (sagging is positive)

0	0.82308	1.5595	2.2093	2.7725	3.249
	3.6389	3.9421	4.1587	4.2887	4.332
	4.2887	4.1587	3.9421	3.6389	3.249
	2.7725	2.2093	1.5595	0.82308	0

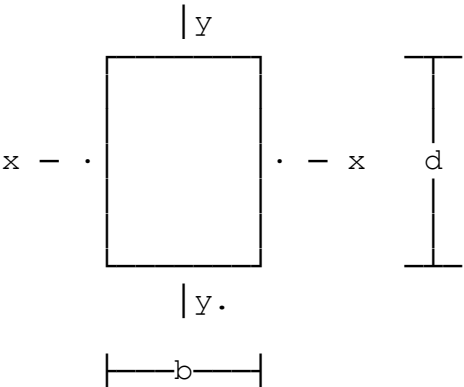
Maximum span bending moment  $4.332\text{ kNm}$

End shears

Shear force at left hand end  $4.56\text{ kN}$   
Shear force at right hand end  $4.56\text{ kN}$   
Design shear force  $F_{ve}'=4.56$

Unfactored dead shear at LHE  $2.66\text{ kN}$   
Unfactored imposed shear at LHE  $1.9\text{ kN}$   
Unfactored dead shear at RHE  $2.66\text{ kN}$   
Unfactored imposed shear at RHE  $1.9\text{ kN}$

Section design parameters



Design bending moment	M=4.332 kNm
Design shear force	Fve=4.56 kN
Design axial load (+ve compress)	Fa=0 kN
Depth of section	d=225 mm
Width of section	b=75 mm
Eff length for bending about xx	Lex=3800 mm
Eff length for bending about yy	Ley=0 mm
Length of bearing	lb=75 mm
From BS5268-2 Table 18, bearing is	< 75 mm from joist end.
Bearing Modification factor	K4=1.0
Strength class C24 to Table 8	
Timber service class adopted	tmclass=1
Timber service class modification factor	K2=1 as Table 16.
Modification factors:	
Bending parallel to grain	K2ben=1.0
Tension parallel to grain	K2ten=1.0
Compression parallel to grain	K2com=1.0
Compression $\perp$ to grain	K2per=1.0
Shear parallel to grain	K2shr=1.0
Mean & min modulus of elasticity	K2mod=1.0

#### Section properties

Inertia about xx axis	$I_x = b \cdot d^3 / 12 = 75 \cdot 225^3 / 12 = 71.191E6 \text{ mm}^4$
Inertia about yy axis	$I_y = d \cdot b^3 / 12 = 225 \cdot 75^3 / 12 = 7.9102E6 \text{ mm}^4$
Area of cross section	$A = b \cdot d = 75 \cdot 225 = 16875 \text{ mm}^2$
Radius of gyration about xx axis	$i_x = \sqrt{I_x / A} = \sqrt{71.191E6 / 16875} = 64.952 \text{ mm}$
Radius of gyration about yy axis	$i_y = \sqrt{I_y / A} = \sqrt{7.9102E6 / 16875} = 21.651 \text{ mm}$

#### Slenderness

Slenderness ratio about xx axis	$\lambda_{bdx} = L_{ex} / i_x = 3800 / 64.952 = 58.505$
Slenderness ratio about yy axis	$\lambda_{bdy} = L_{ey} / i_y = 0 / 21.651 = 0$
xx axis controls slenderness at	$\lambda = \lambda_{bdx} = 58.505$

#### Grade stresses

Compression parallel to grain	$c_{parg} = 7.9 \text{ N/mm}^2$
Bending parallel to grain	$b_{parg} = 7.5 \text{ N/mm}^2$
Shear parallel to grain	$s_{parg} = 0.71 \text{ N/mm}^2$
Compression perp to grain	$c_{perd} = 2.4 \text{ N/mm}^2$
Mean modulus of elasticity	$E_{mean} = 10800 \text{ N/mm}^2$
Minimum modulus of elasticity	$E_{min} = 7200 \text{ N/mm}^2$

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### Modification factors

Duration of loading  $K3=1.25$   
Depth factor  $K7=(300/d)^{0.11}=(300/225)^{0.11}=1.0322$   
Member is not in a load-sharing system as defined by Clause 2.9.  
Modulus of elasticity  $E=E_{min}*K2_{mod}=7200*1=7200 \text{ N/mm}^2$   
Load-sharing modification factor  $K8=1.0$   
No notches exist at the support  $K5=1.0$

### Permissible stresses

Permissible bending stress  $\sigma_{mad}=K2_{ben}*K3*K7*K8*\sigma_{parg}=1*1.25*1.0322*1*7.5=9.6764 \text{ N/mm}^2$   
Shear parallel to grain  $\tau_{orad}=K2_{shr}*K3*K5*K8*\sigma_{parg}=1*1.25*1*1*0.71=0.8875 \text{ N/mm}^2$   
Compress perp to grain (no wane)  $\sigma_{bad}=K2_{per}*K3*K4*K8*\sigma_{cperd}=1*1.25*1*1*2.4=3 \text{ N/mm}^2$

### Bending

Applied bending stress  $\sigma=M*1E6*(d/2)/I_x=4.332*1E6*(225/2)/71.191E6=6.8456 \text{ N/mm}^2$

Since  $\sigma \leq \sigma_{mad}$  (  $6.8456 \text{ N/mm}^2 \leq 9.6764 \text{ N/mm}^2$  ) applied bending stress within permissible.

### Check for deflection (including shear defln as reqd by Clause 2.10.7)

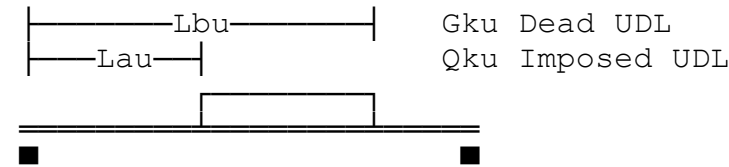
Deflection based on  $E=7200 \text{ N/mm}^2$   
DL deflection without shear  $d_{ld}=d_{ld}=7.4155 \text{ mm}$   
Imposed deflection without shear  $i_{ld}=i_{ld}=5.2968 \text{ mm}$   
Total DL & imposed deflection  $12.712 \text{ mm}$   
Modulus of rigidity  $G=E/16=7200/16=450 \text{ N/mm}^2$   
Shape factor for rect section  $KF=1.2$   
Shear area for beam  $A_y=d*b/KF=225*75/1.2=14062 \text{ mm}^2$   
Total DL & imposed  $9.12 \text{ kN}$   
If total DL & imposed load applied as a UDL, additional deflection due to shear  $d_{su}=W T' * L * 10^6 / (8 * A_y * G)=9.12 * 3.8 * 10^6 / (8 * 14062 * 450)=0.68456 \text{ mm}$   
Shear deflection  $d_{els}=d_{su} * M / (W T' * L / 8)=0.68456 * 4.332 / (9.12 * 3.8 / 8)=0.68456 \text{ mm}$   
Limiting deflection  $DEL_{lim}=0.003 * L * 10^3=0.003 * 3.8 * 10^3=11.4 \text{ mm}$   
Deflection inclusive of shear  $DEL=d_{ld}+i_{ld}+d_{els}=7.4155+5.2968+0.68456=13.397 \text{ mm}$   
Since  $DEL > DEL_{lim}$  (  $13.397 \text{ mm} > 11.4 \text{ mm}$  ), deflection exceeds limiting value.

Location: Brown Edge

Timber beam to BS5268-2:2002



Beam span  $L=2.7\text{ m}$   
All loads are positive downwards, reactions are positive upwards, sagging moments are positive.



Distances are measured from left hand support

Uniformly distributed load 1 of 1  
Dist. from left support to start  $Lau(1)=0\text{ m}$   
Distance from left support to end  $Lbu(1)=2.7\text{ m}$   
Dead load (unfactored)  $Gku(1)=1.15\text{ kN/m}$   
Imposed load (unfactored)  $Qku(1)=3.45\text{ kN/m}$

BMs at 20th points, from left to right (sagging is positive)

0	0.79643	1.509	2.1378	2.6827	3.1438
	3.5211	3.8145	4.0241	4.1498	4.1918
	4.1498	4.0241	3.8145	3.5211	3.1438
	2.6827	2.1378	1.509	0.79643	0

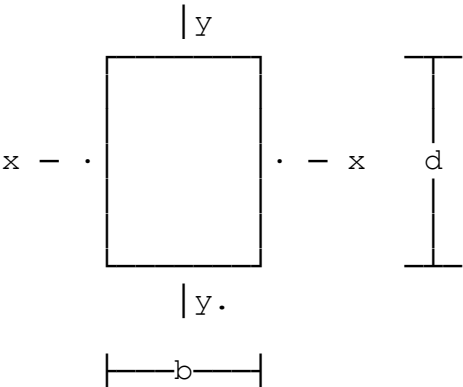
Maximum span bending moment 4.1918 kNm

End shears

Shear force at left hand end 6.21 kN  
Shear force at right hand end 6.21 kN  
Design shear force  $F_{ve}'=6.21$

Unfactored dead shear at LHE 1.5525 kN  
Unfactored imposed shear at LHE 4.6575 kN  
Unfactored dead shear at RHE 1.5525 kN  
Unfactored imposed shear at RHE 4.6575 kN

Section design parameters





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Design bending moment	M=4.1918 kNm
Design shear force	Fve=6.21 kN
Design axial load (+ve compress)	Fa=0 kN
Depth of section	d=225 mm
Width of section	b=75 mm
Eff length for bending about xx	Lex=2700 mm
Eff length for bending about yy	Ley=0 mm
Length of bearing	lb=75 mm
From BS5268-2 Table 18, bearing is	< 75 mm from joist end.
Bearing Modification factor	K4=1.0
Strength class C24 to Table 8	
Timber service class adopted	tmclass=1
Timber service class modification factor	K2=1 as Table 16.
Modification factors:	
Bending parallel to grain	K2ben=1.0
Tension parallel to grain	K2ten=1.0
Compression parallel to grain	K2com=1.0
Compression $\perp$ to grain	K2per=1.0
Shear parallel to grain	K2shr=1.0
Mean & min modulus of elasticity	K2mod=1.0

#### Section properties

Inertia about xx axis	$I_x = b \cdot d^3 / 12 = 75 \cdot 225^3 / 12 = 71.191E6 \text{ mm}^4$
Inertia about yy axis	$I_y = d \cdot b^3 / 12 = 225 \cdot 75^3 / 12 = 7.9102E6 \text{ mm}^4$
Area of cross section	$A = b \cdot d = 75 \cdot 225 = 16875 \text{ mm}^2$
Radius of gyration about xx axis	$i_x = \sqrt{I_x / A} = \sqrt{71.191E6 / 16875} = 64.952 \text{ mm}$
Radius of gyration about yy axis	$i_y = \sqrt{I_y / A} = \sqrt{7.9102E6 / 16875} = 21.651 \text{ mm}$

#### Slenderness

Slenderness ratio about xx axis	$\lambda_{bdx} = L_{ex} / i_x = 2700 / 64.952 = 41.569$
Slenderness ratio about yy axis	$\lambda_{bdy} = L_{ey} / i_y = 0 / 21.651 = 0$
xx axis controls slenderness at	$\lambda = \lambda_{bdx} = 41.569$

#### Grade stresses

Compression parallel to grain	$c_{parg} = 7.9 \text{ N/mm}^2$
Bending parallel to grain	$b_{parg} = 7.5 \text{ N/mm}^2$
Shear parallel to grain	$s_{parg} = 0.71 \text{ N/mm}^2$
Compression perp to grain	$c_{perd} = 2.4 \text{ N/mm}^2$
Mean modulus of elasticity	$E_{mean} = 10800 \text{ N/mm}^2$
Minimum modulus of elasticity	$E_{min} = 7200 \text{ N/mm}^2$

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### Modification factors

Duration of loading  $K3=1.00$   
Depth factor  $K7=(300/d)^{0.11}=(300/225)^{0.11}$   
 $=1.0322$   
Member is not in a load-sharing system as defined by Clause 2.9.  
Modulus of elasticity  $E=E_{min}*K2_{mod}=7200*1=7200 \text{ N/mm}^2$   
Load-sharing modification factor  $K8=1.0$   
No notches exist at the support  $K5=1.0$

### Permissible stresses

Permissible bending stress  $\sigma_{mad}=K2_{ben}*K3*K7*K8*\sigma_{parg}$   
 $=1*1*1.0322*1*7.5$   
 $=7.7411 \text{ N/mm}^2$   
Shear parallel to grain  $\tau_{orad}=K2_{shr}*K3*K5*K8*\tau_{sparg}$   
 $=1*1*1*1*0.71$   
 $=0.71 \text{ N/mm}^2$   
Compress perp to grain (no wane)  $\sigma_{bad}=K2_{per}*K3*K4*K8*\tau_{cperd}$   
 $=1*1*1*1*2.4$   
 $=2.4 \text{ N/mm}^2$

### Bending

Applied bending stress  $\sigma=M*1E6*(d/2)/I_x$   
 $=4.1918*1E6*(225/2)/71.191E6$   
 $=6.624 \text{ N/mm}^2$

Since  $\sigma \leq \sigma_{mad}$  (  $6.624 \text{ N/mm}^2 \leq 7.7411 \text{ N/mm}^2$  ) applied bending stress within permissible.

### Check for deflection (including shear defln as reqd by Clause 2.10.7)

Deflection based on  $E=7200 \text{ N/mm}^2$   
DL deflection without shear  $d_{ld}=d_{ld}=1.5525 \text{ mm}$   
Imposed deflection without shear  $i_{ld}=i_{ld}=4.6575 \text{ mm}$   
Total DL & imposed deflection  $6.21 \text{ mm}$   
Modulus of rigidity  $G=E/16=7200/16=450 \text{ N/mm}^2$   
Shape factor for rect section  $KF=1.2$   
Shear area for beam  $A_y=d*b/KF=225*75/1.2=14062 \text{ mm}^2$   
Total DL & imposed  $12.42 \text{ kN}$   
If total DL & imposed load applied as a UDL, additional deflection due to shear  $d_{su}=W T' * L * 10^6 / (8 * A_y * G)$   
 $=12.42 * 2.7 * 10^6 / (8 * 14062 * 450)$   
 $=0.6624 \text{ mm}$   
Shear deflection  $d_{els}=d_{su} * M / (W T' * L / 8)$   
 $=0.6624 * 4.1918 / (12.42 * 2.7 / 8)$   
 $=0.6624 \text{ mm}$   
Limiting deflection  $DEL_{lim}=0.003 * L * 10^3 = 0.003 * 2.7 * 10^3$   
 $=8.1 \text{ mm}$   
Deflection inclusive of shear  $DEL=d_{ld}+i_{ld}+d_{els}=1.5525+4.6575+0.6624$   
 $=6.8724 \text{ mm}$   
Since  $DEL \leq DEL_{lim}$  (  $6.8724 \text{ mm} \leq 8.1 \text{ mm}$  ), OK for deflection.

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Shear and bearing

Shear stress (no notches)       $tora = 3 * Fve * 1000 / (2 * b * d)$   
    $= 3 * 6.21 * 1000 / (2 * 75 * 225)$   
    $= 0.552 \text{ N/mm}^2$

Since  $tora \leq torad$  (  $0.552 \text{ N/mm}^2 \leq 0.71 \text{ N/mm}^2$  ) shear stress  
does not exceed permissible therefore OK.

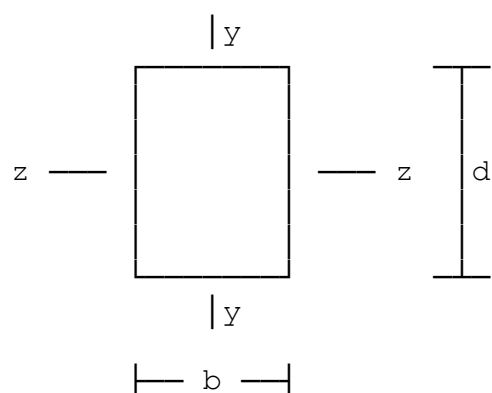
Bearing stress on wall plate       $sigba = Fve * 1000 / (lb * b)$   
    $= 6.21 * 1000 / (75 * 75)$   
    $= 1.104 \text{ N/mm}^2$

Since  $sigba \leq sigbad$  (  $1.104 \text{ N/mm}^2 \leq 2.4 \text{ N/mm}^2$  ) bearing stress  
does not exceed permissible therefore OK.

	Member: 225 mm x 75 mm
	Strength class C24 to Table 8
	Moisture service class 1
	Bending stress      6.624 N/mm <sup>2</sup>
	Permissible bending      7.7411 N/mm <sup>2</sup>
DESIGN	Deflection      6.8724 mm
SUMMARY	Limiting deflection      8.1 mm
	Shear stress      0.552 N/mm <sup>2</sup>
	Permissible shear      0.71 N/mm <sup>2</sup>
	Bearing stress      1.104 N/mm <sup>2</sup>
	Permissible bearing      2.4 N/mm <sup>2</sup>

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Location: Brown Edge



Rectangular timber member

subject to axial load and

bending about z-z axis

Calculations in accordance  
with BS5268-2:2002.

Design BM about zz (positive)	$M_z = 1.5 \text{ kNm}$
Design shear force in y direction	$V = 0 \text{ kN}$
Design axial load (+ve compress)	$F = 15.5 \text{ kN}$
Member is in compression.	
Eff length for bending about zz	$L_{ez} = 1.800 \text{ m}$
Depth of section	$d = 150 \text{ mm}$
Width of section	$b = 150 \text{ mm}$
	$L_{ez} = L_{ez}' * 1000 = 1.8 * 1000 = 1800 \text{ mm}$
Eff length for bending about yy	$L_{ey} = 1.8 \text{ m}$
	$L_{ey} = L_{ey}' * 1000 = 1.8 * 1000 = 1800 \text{ mm}$
Strength class C24 to Table 8	

### Section properties

Largest section dimension	$h = b = 150 \text{ mm}$
Inertia about zz axis	$I_z = b * d^3 / 12 = 150 * 150^3 / 12$ $= 42.188 \text{E}6 \text{ mm}^4$
Inertia about yy axis	$I_y = d * b^3 / 12 = 150 * 150^3 / 12$ $= 42.188 \text{E}6 \text{ mm}^4$
Area of cross section	$A = b * d = 150 * 150 = 22500 \text{ mm}^2$
Radius of gyration about zz axis	$i_z = \text{SQR}(I_z / A) = \text{SQR}(42.188 \text{E}6 / 22500)$ $= 43.301 \text{ mm}$
Radius of gyration about yy axis	$i_y = \text{SQR}(I_y / A) = \text{SQR}(42.188 \text{E}6 / 22500)$ $= 43.301 \text{ mm}$

### Slenderness

Slenderness ratio about zz axis	$\lambda_{bdz} = L_{ez} / i_z = 1800 / 43.301$ $= 41.569$
Slenderness ratio about yy axis	$\lambda_{bdy} = L_{ey} / i_y = 1800 / 43.301$ $= 41.569$
yy axis controls SR	$\lambda_{bda} = \lambda_{bdy} = 41.569$

Grade stresses

Compression parallel to grain	$c_{parg}=7.9 \text{ N/mm}^2$
Bending parallel to grain	$b_{parg}=7.5 \text{ N/mm}^2$
Shear parallel to grain	$s_{parg}=0.71 \text{ N/mm}^2$
Mean modulus of elasticity	$E_{mean}=10800 \text{ N/mm}^2$
Minimum modulus of elasticity	$E_{min}=7200 \text{ N/mm}^2$

Modification factors

Timber service class adopted  $tmclass=3$   
Timber stress grades and moduli adjusted as table 16.  
Modification factors:  
Bending parallel to grain  $K2ben=0.8$   
Tension parallel to grain  $K2ten=0.8$   
Compression parallel to grain  $K2com=0.6$   
Compression  $\perp$  to grain  $K2per=0.6$   
Shear parallel to grain  $K2shr=0.9$   
Mean & min modulus of elasticity  $K2mod=0.8$   
Duration of loading  $K3=1.00$   
Depth factor  $K7=(300/d)^{0.11}=(300/150)^{0.11}=1.0792$   
Member is not in a load-sharing system as defined by Clause 2.9.  
Modulus of elasticity  $E=E_{min}*K2mod=7200*0.8=5760 \text{ N/mm}^2$   
Load-sharing modification factor  $K8=1.0$

For compression members with slenderness ratios equal to or greater than 5, the permissible stress should be calculated as the product of the grade compression parallel to the grain stress, modified as appropriate for size, moisture content, duration of load and load sharing, and the modification factor  $K12$  given by table, or calculated as follows using the equation in annex B. The value of modulus of elasticity should be the minimum modulus of elasticity. The compression parallel to the grain stress required for entry to annex B should be the grade stress modified only for moisture content and duration of load.

Compr. parallel to grain stress  $sigc=K2com*K3*c_{parg}=0.6*1*7.9=4.74 \text{ N/mm}^2$   
Modulus of elasticity  $E=E_{min}*K2mod=7200*0.8=5760 \text{ N/mm}^2$   
Factor for annex B  $C=PI^2*E/(1.5*\lambda^2*sigc)=3.1416^2*5760/(1.5*41.569^2*4.74)=4.6271$   
Eccentricity factor  $\eta=0.005*\lambda=0.005*41.569=0.20785$   
Modification factor  $K12=(0.5+(1+\eta)*C/2)-((0.5+(1+\eta)*C/2)^2-C)^{0.5}=(0.5+(1+0.20785)*4.6271/2)-((0.5+(1+0.20785)*4.6271/2)^2-4.6271)^{0.5}=0.79921$

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## Permissible stresses

$$\begin{aligned} \text{Permissible compression stress} \quad \sigma_{\text{cad}} &= K_2 \cdot \sigma_{\text{com}} \cdot K_3 \cdot K_8 \cdot K_{12} \cdot c_{\text{parg}} \\ &= 0.6 \cdot 1 \cdot 1 \cdot 0.79921 \cdot 7.9 \\ &= 3.7882 \text{ N/mm}^2 \end{aligned}$$

Permissible bending stress  $\sigma_{\text{adm}} = K_2 \cdot \sigma_{\text{ben}} \cdot K_3 \cdot K_7 \cdot K_8 \cdot b_{\text{parg}}$   
 $= 0.8 \cdot 1 \cdot 1.0792 \cdot 1 \cdot 7.5$   
 $= 6.4754 \text{ N/mm}^2$

Axial compression

The limitation on bow in most stress grading rules are inadequate for the selection of material for columns. Particular attention should therefore be paid to the straightness of columns, e.g. by limiting bow to approximately  $1/300$  of the length.

[illegible]

## Bending

Applied bending stress  $\sigma = Mz \cdot 1E6 \cdot (d/2) / I_z$   
 $= 1.5 \cdot 1E6 \cdot (150/2) / 42.188E6$   
 $= 2.6667 \text{ N/mm}^2$

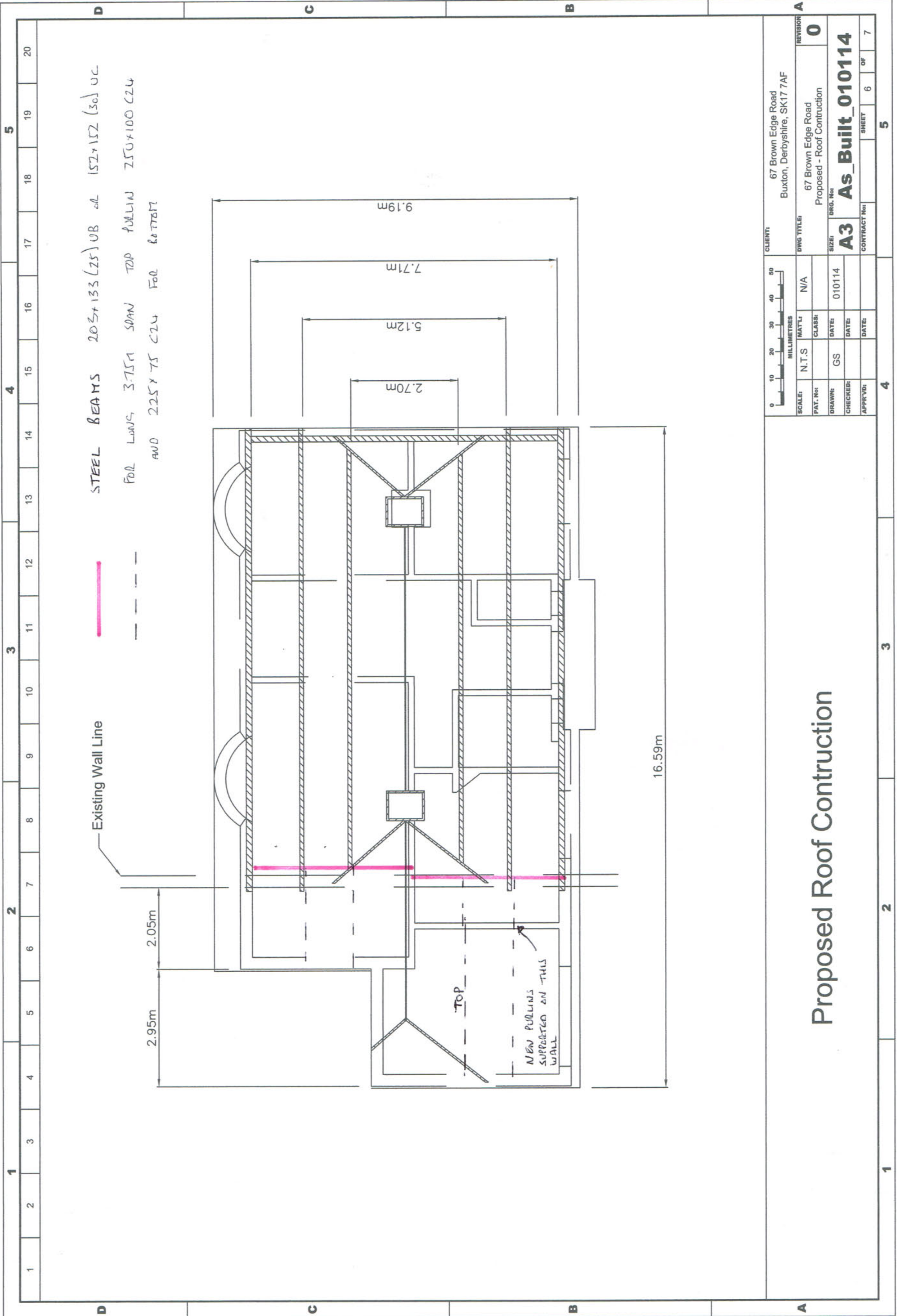
```
Euler critical stress      sige=PI^2*E/lambda^2  
                           =3.1416^2*5760/41.569^2  
                           =32.899 N/mm^2
```

Bending stress modification fact    bsmf=1-1.5\*sigca\*Kl2/sige  
    =1-1.5\*0.68889\*0.79921/32.899  
    =0.9749

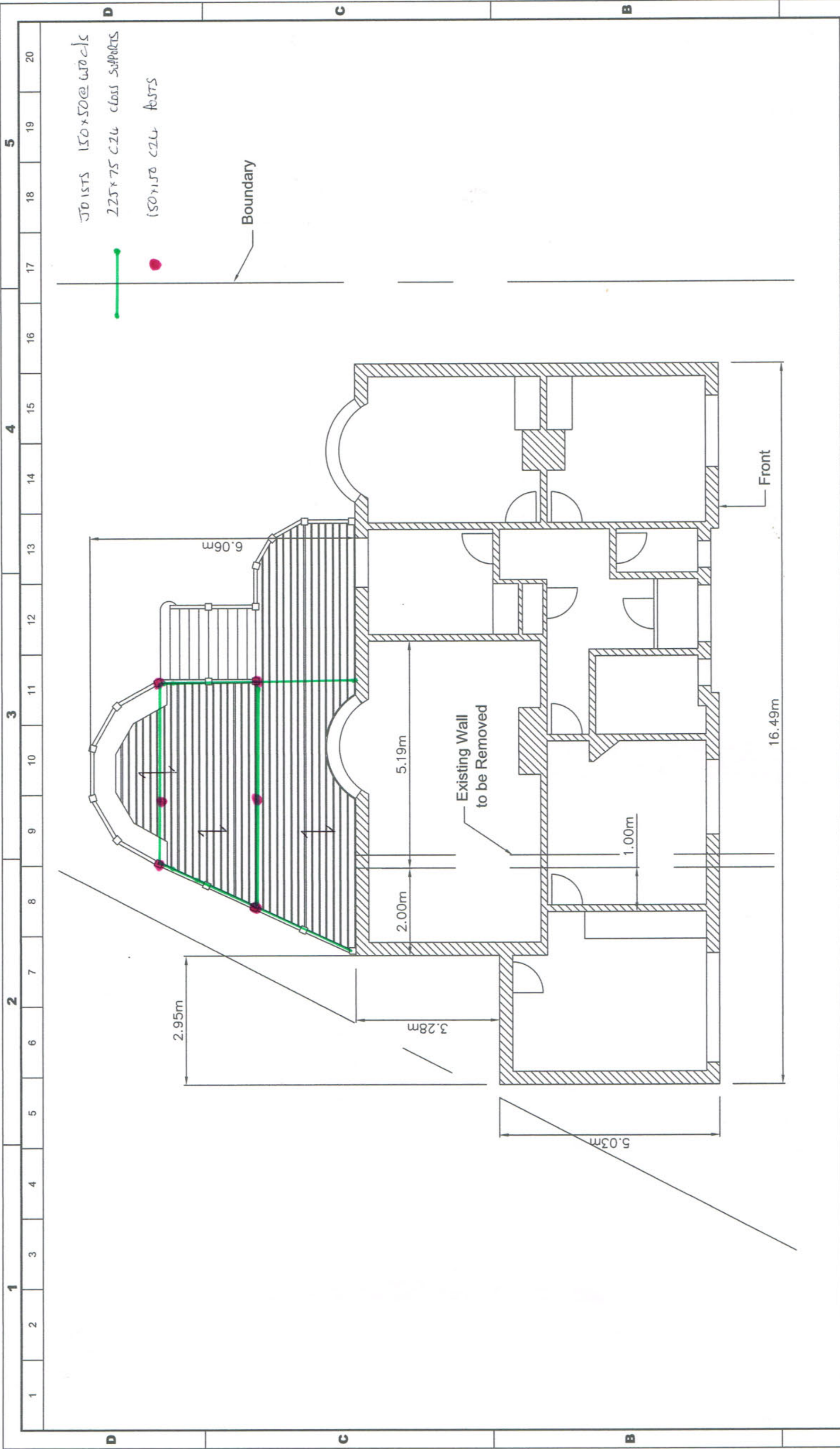
```
Interaction factor      factor=sigma/(sigmad*bsmf)+sigca
                        /sigcad
                        =2.6667/(6.4754*0.9749)
                        +0.68889/3.7882
                        =0.60427
```

Interaction factor less than or equal to unity therefore OK.

DESIGN SUMMARY	Depth of section	150 mm
	Width of section	150 mm
	Strength class	C24 to Table 8
	Timber moisture class	3
	Applied comprn stress	0.68889 N/mm <sup>2</sup>
	Permiss comprn stress	3.7882 N/mm <sup>2</sup>
	Applied bending stress	2.6667 N/mm <sup>2</sup>
	Permiss bending stress	6.4754 N/mm <sup>2</sup>
	Interaction factor	0.60427



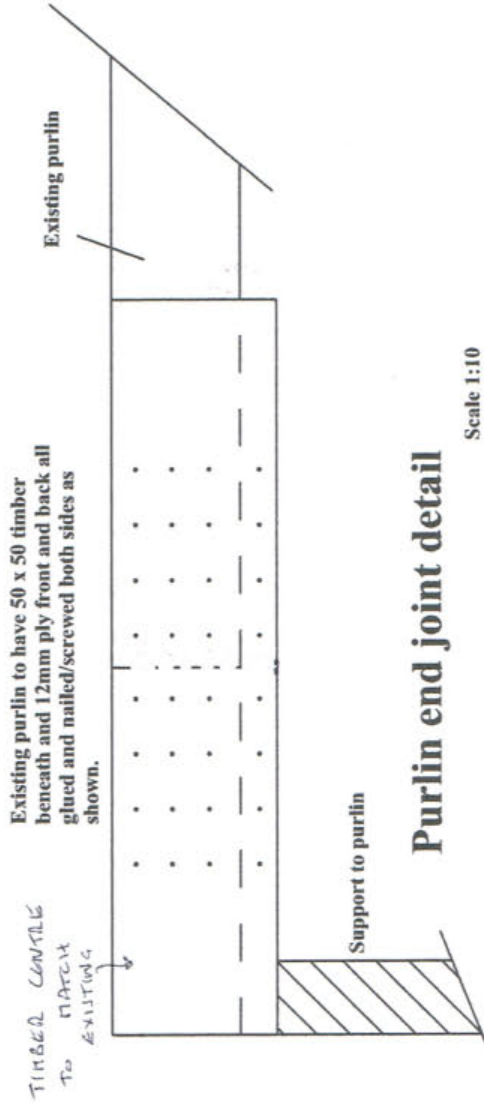




CLIENT: 67 Brown Edge Road Buxton, Derbyshire, SK17 7AF										67 Brown Edge Road Proposed - Plan View									
DWG TITLE: 67 Brown Edge Road Proposed - Plan View										REVISION: 0									
SIZE: A3										DRG. No: 010114									
CONTRACT No: 010114										SHEET 5 OF 7									
SCALE: N.T.S.										MATERIAL: N/A									
PAT. No: GS										CLASS: 010114									
DRAWN: GS										DATE: 010114									
CHECKED:										DATE:									
APPROVED:										DATE:									

Proposed Plan View





**Purlin end joint detail**

Scale 1:10

FIGURE 1